

Learning Effective Sparse Sampling Strategies using Deep Active Sensing

Mehdi Stapleton^{1,2}, Dieter Schmalstieg¹, Clemens Arth^{1,2}, and Thomas Gloor³

¹ICG, Graz University of Technology, Inffeldgasse 16/2, 8010 Graz, Austria

²AR4 GmbH, Strauchergasse 13, 8020 Graz, Austria

³Hilti Corporation, Feldkircherstrasse 100, 9494 Schaan, Liechtenstein
{mehdi.stapleton, dieter, arth}@icg.tugraz.at, thomas.gloor@hilti.com

Keywords: Sparse Registration, Active Perception, Active Localization, General Hough Transform

Abstract: Registering a known model with noisy sample measurements is in general a difficult task due to the problem in finding correspondences between the samples and points on the known model. General frameworks exist, such as variants of the classical iterative closest point (ICP) method to iteratively refine correspondence estimates. However, the methods are prone to getting trapped in locally optimal configurations, which may be far from the true registration. The quality of the final registration depends strongly on the set of samples. The quality of the set of sample measurements is more noticeable when the number of samples is relatively low (≈ 20). We consider sample selection in the context of *active perception*, i.e. an objective-driven decision-making process, to motivate our research and the construction of our system. We design a system for learning how to *select* the regions of the scene to sample, and, in doing so, improve the accuracy and efficiency of the sampling process. We present a full environment for learning how best to sample a scene in order to quickly and accurately register a model with the scene. This work has broad applicability from the fields of geodesy to medical robotics, where the cost of taking a measurement is much higher than the cost of incremental changes to the pose of the equipment.

1 INTRODUCTION

Localization within a new scene requires aligning observed elements of the scene with prior knowledge of the environment. The process is relevant to a wide-ranging group of disciplines from Robotic Navigation to Augmented Reality. When given a prior model of the environment, the process is termed model-based registration.

Classical approaches to model-based registration rely on dense-sampling of the scene using dense sensors, e.g., laser scanners, followed by optimization routines to register the model with the observations (Ballard, 1981). However, the nonlinear nature of the optimization routine leaves it prone to local optima and sensitive to initialization – i.e., the original sampling of the scene (Rusinkiewicz and Levoy, 2001). Given the importance of the original sampling, many works have attempted to tackle the problem via geometry-based reductions of the original dense-sampling to prevent spurious local optima (Rusinkiewicz and Levoy, 2001). Sparse-sampling of the scene has received considerably less attention, as a small number of samples poses difficulties for ef-

fective reductions of the sample-set (Arun Srivatsan et al., 2019). Sparse-sampling strategies will typically be employed in cases where a single-measurement is expensive either with regards to time taken or energy consumed. Due to the effective limit on the number of samples to be taken, sparse-sampling processes must be judicious in their selection of good vantage points.

In this paper, we present an algorithm for effectively sparse-sampling the environment to register it with respect to a given model, i.e. *model-based registration*. We consider polygonal floor-plan models, e.g. common in industrial construction and surveying applications. We will present an approach based on recent work using Active Localization (Chaplot et al., 2018), combined with integration into a robust method for localization. The algorithm will be a two-stage approach. The first stage comprises carrying out a robust and noise-tolerant sparse-sampling strategy in a new environment. The second stage will refine the registration using efficient sparse-registration techniques (Arun Srivatsan et al., 2019). We will demonstrate the effectiveness of our approach on sample floor-plans, and present interpretations of the sampling strategies.

2 RELATED WORK

Our approach learns active sampling strategies for quickly and accurately registering a surrounding scene with a model of the environment. The work thereby lies at the intersection of active sensing and geometric sub-sampling techniques.

2.1 Iterative-Closest-Point (ICP)

The work of Rusinkiewicz and Levoy (2001) formalized the general process of ICP into six parts: point-selection, neighbourhood-selection, point-matching, weighting pairs, outlier rejection, and error minimization. They emphasize the importance of the earlier stages in order to guarantee that the final error minimization would be well-conditioned. ICP techniques are typically performed on dense point sets, which helps to *smooth out* any sub-optimal behaviour in the earlier parts. Evidently, the earlier parts, including point-selection, become especially important when we have a sparse number of measurements.

In the context of point-set registration (PSR), many works have investigated different methods of point-selection as means of constraining the downstream error minimization routine. Early works to address this point-selection have looked at geometrically stable model points (Gelfand et al., 2003), the sampling of a diverse distribution of points based on intrinsic point characteristics such as normal-vector (Rusinkiewicz and Levoy, 2001), and selection of points based on constraining motion in a local neighbourhood of the point (Torsello et al., 2011).

It is along this line of research that we propose a system for learning how best to select sample points in a scene. The aforementioned methods are largely based on sub-sampling a captured dense point-set of a target object, and leveraging *a priori* knowledge of how *geometry* plays with registration. Unlike these methods, we learn a *policy* on how to perform point-selection in an *online* manner. Moreover, we learn to make decisions on whether or not to sample certain regions of the scene based solely on our prior samples and a binary detector for topologically interesting scene content.

Along with point-selection for registration, we also simultaneously consider a dual-objective: we would like to perform a point-selection in a minimal amount of time as possible. Given a fixed time cost to performing a measurement and moving the agent, this can be reformulated as finding a minimal set of points for accurate registration. In this respect, we may consider our objective similar to active-sensing: We aim to minimize the uncertainty in our registration belief-space with each sample measurement.

2.2 Active localization

Active Markov Localization (AML), popularized by the work of Fox et al. (1998), takes an *active* approach to controlling the robots actions in order to minimize the expected future entropy of the system. This work uses a grid for storing the belief of the robot pose. Due to the large-size of the grid for moderate scene sizes, efficient optimizations are needed to run the algorithm. Foremost, the measurement likelihood is pre-computed for every location within the grid, so that the belief update corresponds to a handful of table lookups. Another optimization is the belief map is assumed to condense to only a small number of possible poses. Hence only the neighbourhoods about those probable locations need to be considered. Similarly, we use a grid-based localization scheme, but we would like to avoid the onerous pre-computation phase. We instead use a General Hough Transform style method for updating our belief.

The more recent Active Monte Carlo Localization (AMCL) work of Kümmerle et al. (2008) uses a particle filter for representing the belief. To avoid costly ray-cast operations for each particle to evaluate the information gain of a given action, the particles are grouped into clusters. Each cluster then performs a ray-cast operation from the mean of the cluster in the information gain, i.e., utility function (Fox et al., 1998).

2.3 Deep Reinforcement Learning

The work of Chaplot et al. (2018) and Gottipati et al. (2019) specifically look at this dual-objective in the context of active localization; a robotic agent must determine its position within a map. Chaplot et al. (2018) consider a robotic agent which can move in four directions (up, down, right, left) with a forward facing depth sensor. The work uses a fixed grid to store the belief of the robotic location within a maze and uses the belief map in its state representation. We similarly use a belief map in our state representation; however we use a novel grid-based localization algorithm for generating the belief map.

Gottipati et al. (2019) train a residual neural network to learn the likelihood map for a given state-action pair via supervised learning, which it then uses to update the prior belief during operation. The robotic agent is equipped with a 360° laser scanner, which is used as the measurement device. In contrast, our system uses a *limited* observation mechanism which is simply a binary topological indicator which coarsely highlights areas of wall intersections. Our work additionally considers registration error with our objective to find a minimal set as quickly

as possible. Moreover, both prior works look at the maximum of the belief map at the ground-truth pose as the maximization objective; whereas we strive to minimize the final registration error and the trajectory cost (i.e., agent motion and measurement time penalties).

2.4 Discussion

Our method’s computational cost is dependent on the perimeter of the map as opposed to the interior. In most scenes, the perimeter of the map is significantly smaller than the interior area; hence we can expect significant computational savings. Since we are considering problems with a sparse number of measurements possibly containing noise and outliers, we cannot readily disqualify regions of the belief space which may have gotten little consideration after the first handful of samples. Therefore, we need to consider the whole belief space throughout our active-sensing routine. This means the sparse sampling problem is ill-suited for optimizations which only consider a handful of poses early-on in the algorithm.

We claim the following contributions:

- A system for learning active-sampling strategies which considers both efficiency and accuracy for the registration of a scene with a known model.
- A novel grid-based localization scheme, with lower front-end computational load than classical approaches.
- A full simulation environment for learning active-sampling strategies, which includes map generation, localization, sparse-registration, and a symmetry-aware evaluation module.
- An inspection tool for investigating *deep* policy behaviour elicited by our active sampling strategy.

3 METHODOLOGY

We design a system for effectively sampling the surrounding scene in a sparse manner. The sampling strategy is learnt via a reinforcement-learning approach. Hence, we adopt the following terminology: the *agent* denotes the entity performing the sampling, the *environment* refers to the 2D or 3D scene surrounding the agent, and the *policy* $\pi(a|s)$ refers to how the probability of the agent selecting an action a given the current state s of the system.

The system is composed of four modules:

1. Our fast localization module, responsible for coarsely hypothesizing the likelihood of the agent’s pose within the environment
2. The active-sampling module, decides how to take sample measurements
3. The refinement module, responsible for sparse-registration of the scene with the model given a coarse estimate
4. The evaluation module for assessing in a symmetry-aware fashion the quality of the final registration

We also introduce an inspection tool for easily investigating the decision-making process of the active-sampling module.

The sub-systems, shown in Figure 1, work in concert in order to quickly and accurately register a known model with the judiciously selected sample measurements of the environment. We develop a simulation environment which generates outlines for random floor-plans. The outlines represent single indoor room scenes. We do not consider furniture or other obstacles between the measurement device and the walls of the room. Thereby, we concentrate on learning sampling strategies based purely on the room geometry. We allow the floor-plan outline to be a simple non-convex polygon. The measurement device is assumed to be level with respect to the ground-plane of the simulated room, which can be achieved in practice by aligning the negative z-axis of the device reference frame with respect to the gravity vector given by an on-board accelerometer. The simulation places the agent (i.e., measurement device) at a random location about the *visual center* of the room.

We use a quad-tree based algorithm to quickly compute the visual center of our floor-plan. The distance between the visual center and the nearest wall of the floor-plan determines the radius of a uniform distribution about the visual center for placement of the agent. We proceed to detail each individual sub-system in the following sections in order of appearance in our pipeline.

3.1 Learning sampling strategies

We frame the problem of effective sampling as a Partially-Observed Markov Decision Process (POMDP). In this process, the agent must learn a policy which maximizes the expected cumulative reward ($\mathbb{E}[\mathbf{R}]$) over the course of an episode (τ). An episode consists of a sequence of actions, which are drawn from a discrete action set, until completion of a task or allotted *time*. We design a reward signal which penalizes excessively *lengthy* action sequences and re-

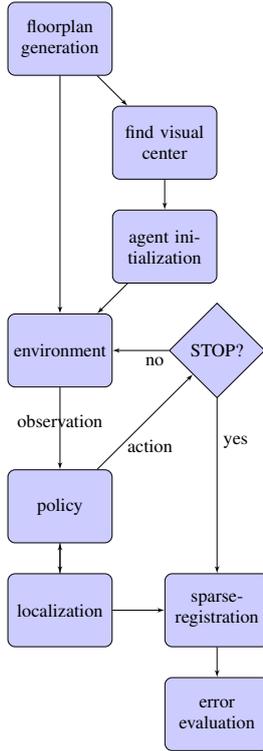


Figure 1: System overview of our environment. We provide a simulation environment for generating floor-plans. The agent is initialized within room, about the visual center. A learnt policy then interacts with the environment via the agent’s actions and makes observations of the scene. During interactions, a belief map maintains a coarse distribution over the likely pose of the model with respect to the scene. Once the policy dictates termination, then the current coarse estimate is fed to the sparse-registration module for refinement of our registration of the model with respect to the scene. Finally, we evaluate the error using a symmetry-aware pose-distance.

wards low final registration error (Sections 3.2 and 3.3). Each action from the discrete set has an intrinsic cost. In practice, the cost of a measurement action greatly outweighs the cost of a small robotic manipulation of the agent (e.g., change of pose of the on-board sensor). We observe this behaviour in any robotic platform outfitted with a high accuracy measurement device, e.g., electronic distance measurement (EDM) devices used in surveying applications, which are designed for reliable and robust operation. The *length* of an action sequence measures the sum of action costs, e.g., expensive measurement actions and cheap rotations. By penalizing the length of the action sequence, we elicit behaviour which strives to find a correct registration as quickly as possible. The cost associated with the accuracy of the final registration provides a natural negative feedback mechanism for the *length*. This feedback mitigates the agent learn-

ing shortcuts to a quick-and-dirty registration, which is ill-suited for proceeding to sparse registration refinement, or prone to getting trapped in a local sub-optimum.

We use the coarse registration error as an indicator of episode completion, i.e., once the coarse localization (Section 3.2) is able to approximately register the scene with the model, the action sequence terminates and proceeds to the next stage in the pipeline (Section 3.3). We use the final registration error (i.e., after refinement) to penalize the final reward signal.

Our objective function is the expected cumulative reward $\arg \max_{\pi} \mathbb{E}_{\tau} [\mathbf{R} | \pi]$ with

$$\mathbf{R} = \sum_{t=0}^{T-1} \gamma^t r_t \quad (1)$$

where T is the maximum length of the episode, r_t is the reward at time-step t , and we use a discounted cumulative reward with the discount factor $\gamma \in (0, 1]$. We parameterize our policy using a functional approximator, π_{θ} , with θ denoting the free parameters of our function. Policy gradient methods have been shown to be an effective technique to optimizing Equation 1 (Sutton and Barto, 2018) given we follow the same policy we optimize (i.e., *on-policy* learning). The policy gradient is given as follows,

$$\begin{aligned} \nabla_{\theta} \mathbb{E}_{\tau} [\mathbf{R}] = & \\ \mathbb{E}_{\tau} \left[\sum_{t=0}^{T-1} \nabla_{\theta} \log \pi(a_t | s_t, \theta_t) \left(\sum_{t'=t}^{T-1} \gamma^{t'-t} r_{t'} - V^{\pi}(s_t) \right) \right] & \quad (2) \end{aligned}$$

We express the policy with respect to the parameters θ and emphasize its interpretation as a conditional probability over the next action selection (a_t) given the current state of the system (s_t). Noteworthy, we use the value function V^{π} ,

$$V^{\pi}(s) = \mathbb{E}_{\tau} \left[\sum_{l=0}^{T-t-1} \gamma^l r_{t+l} \mid s_t = s \right] \quad (3)$$

as a *baseline* to reduce the variance of our gradient estimate from Equation 2.

We use the Asynchronous Advantage Actor-Critic (A3C) policy gradient method (Mnih et al., 2016) to maximize the expected cumulative reward. We choose A3C over other contemporary approaches such as proximal policy optimization (PPO) (Schulman et al., 2017) due to the demonstrated efficacy of A3C on a similar class of problems (Chaplot et al., 2018).

The inner term of Equation 2 represents the *advantage* seen for an action sequence over the expected

cumulative reward $V^\pi(s_t)$. Hence, action sequences with positive advantage will act to nudge the parameters to encourage future similar action sequences, whereas a negative advantage, i.e., an observed cumulative reward below baseline, will nudge parameters away from such action sequences. The parameters will act on the individual actions through the log-probability of selecting such an action in a given state. Many algorithms wrestle with providing a reliable estimate of the *advantage* without having to wait until the episode terminates to perform a parameter update. A central *bias-variance* trade-off lies at the heart of algorithm development. Similar to the implementation of Chaplot et al. (2018), we use the Generalized Advantage Estimator (GAE) (Schulman et al., 2015) for computing an estimate. The GAE provides an extra *lever* for controlling the bias-variance trade-off through a parameter λ ,

$$\begin{aligned} \delta_t &= r_t + \gamma V^\pi(s_{t+1}) - V^\pi(s_t) \\ A_t^{\pi,\gamma} &= \sum_{i=0}^{T-t-1} (\gamma\lambda)^i \delta_{t+i} \end{aligned} \quad (4)$$

where $A_t^{\pi,\gamma}$ denotes our estimate of the advantage for time-step t , based on our policy $\pi(a|s)$.

The training procedure performs simulation as previously described, with periodic parameter updates based on the experiences of the most recent *segment* of the episode. Therefore, we perform more frequent policy updates.

We primarily compose our state representation the belief-space of the agent’s pose within the scene, similar to Chaplot et al. (2018), and a history of recent coarse narrow field-of-view (FOV) topological *scans* of the scene from the agent pose. The scans act as a proxy for a conservative wall-intersection detector.

In case of pathological lighting conditions or occlusions, we can at best assume a coarse indicator of a wall intersection within a narrow FOV of the agent’s bearing. We manage the belief-space of the agent’s pose from all sample measurements up to the current time, by using a grid-based localization system of our own design, details in Section 3.2.

As shown in Figure 2, we modify the Actor-Critic architecture of Chaplot et al. (2018) to supply the collection of scans through a fully-connected network along with the current step count within the episode and the recent action history.

3.2 Localization

We design the localization module with multiple considerations in mind. The module should be able to

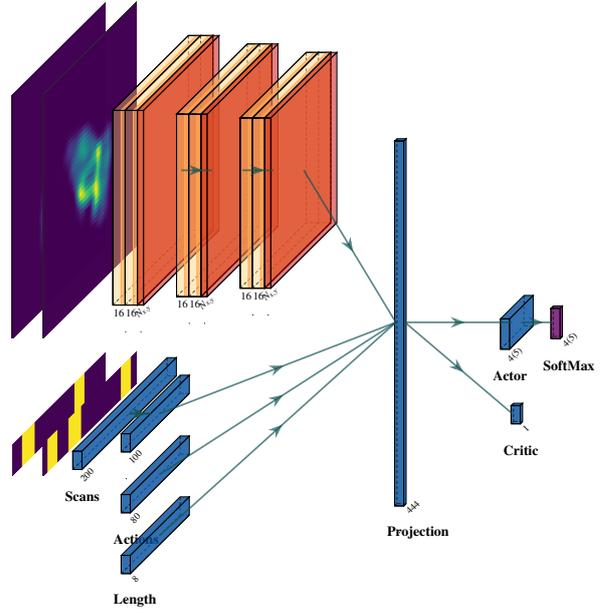


Figure 2: Architecture of our policy model. We modify the architecture of Chaplot et al. (2018) to accommodate our topological scans. The inputs comprise the $|N_x| \times |N_y| \times |N_\xi|$ belief map (Section 3.2) - top left, the recent topological scans, the recent action history, and the current step index in the episode.

withstand noise and especially outliers, as well as providing a good degree of accuracy. Our primary concern is robustness, since the downstream sparse registration module (Section 3.3) will be able to help ensure a final accurate estimate. Due to complete or partial symmetries, the localization technique should be able to accommodate multi-modal belief space distributions. Critically, the module needs to present the belief map over the agent pose in a form digestible by the active-sampling module (Section 3.1). The latter constraint disqualifies classical particle-filter-based localization techniques (Kümmerle et al., 2008, Thrun et al., 2005), due to resultant complexity in communicating the belief, i.e., collection of particles, to the active-sampling module. With all these considerations, we decide to employ a novel Hough Transform-based approach. Specifically, we rely on the Generalized Hough Transform (GHT) (Ballard, 1981) for accumulating votes into the belief over the agent pose.

We consider a fixed grid underlying our grid-based localization scheme. The fixed size reduces the complexity of down-stream processing in the active-sampling module. We define the robot pose by the tuple $\mathbf{x} := (x_w^{\text{offset}}, y_w^{\text{offset}}, \xi_w^a) \in N_x \times N_y \times N_\xi$ representing the translation and the orientation of the agent. We adopt a special convention in light of the use of the GHT. The translation components

$(x_w^{\text{offset}}, y_w^{\text{offset}})$ represent the offset between the agent position (x_w^a, y_w^a) and the centroid of the surrounding scene $(x_w^{\text{scene}}, y_w^{\text{scene}})$ in the world coordinate frame \mathbb{W} . The orientation component ξ_w^a represents the rotation of the agent in the world coordinate frame. An annotated illustration of a sample floor-plan with our labelling convention is shown in Figure 3.

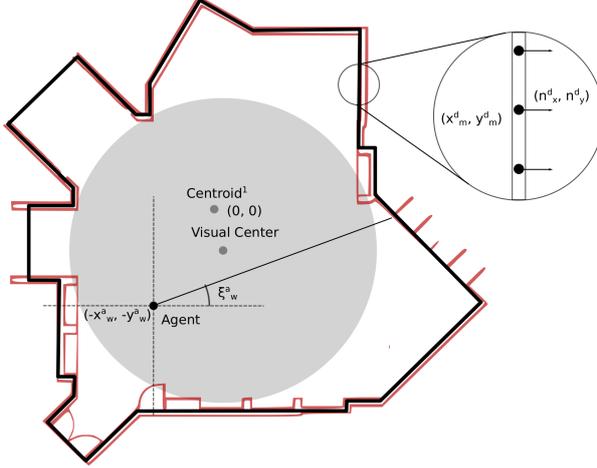


Figure 3: Illustration of floorplan diagram.

The grid dimensions are given as $|N_x| \times |N_y| \times |N_\xi|$. The grid will hold the belief of the robot pose, which will be updated based on the measurement likelihood via classical Bayesian filtering,

$$p(\mathbf{x}_{t+1} | o_{0:t+1}, a_{0:t}) \propto p(o_{t+1} | \mathbf{x}_{t+1}) \int_{\mathbf{x}_t} p(\mathbf{x}_{t+1} | \mathbf{x}_t, a_t) p(\mathbf{x}_t | o_{0:t}, a_{0:t}) d\mathbf{x}_t, \quad (5)$$

where the o_t and a_t are the observation and action taken at time-step t , respectively. Our grid would hold the current belief at each time t , i.e. $p(\mathbf{x}_t | o_{0:t}, a_{0:t})$. At each time-step, a new action is taken, which induces the convolution over the motion model $p(\mathbf{x}_{t+1} | \mathbf{x}_t, a_t)$, and a new observation is taken following the action which weights the motion-updated belief with the measurement likelihood $p(o_{t+1} | \mathbf{x}_{t+1})$. For large grid sizes, the process of applying the time-update and measurement-update can be computationally expensive. Hence, classical approaches must perform several cost-saving measures to run in real-time. Firstly, the measurement likelihood for each cell of the grid is pre-computed, i.e. a ray-casting operation is performed to compute $p(o_{t+1} | \mathbf{x}_{t+1})$ for all $|N_x| \times |N_y| \times |N_\xi|$. Secondly, the belief space is assumed to coalesce around only a small number of modes; hence, only a small number of belief clusters need to be maintained. Essentially, the latter assumption relaxes the grid-based localization to an approximate multiple hypothesis Kalman filter.

The large up-front cost of the ray-casting pre-computations can be prohibitive, especially, for operations where the map may be parametrizable and therefore changes every iteration. Therefore, we want our approach to avoid the large up-front cost, while being able to maintain a real-time computational load during the measurement update phase.

With regards to the previously mentioned relaxation, the assumption of the belief space coalescing around only a small number of modes is, in general, inappropriate for cases where only a sparse number of measurement will be taken overall. In our case, the number of samples is small and each measurement could be corrupted by noise or outliers. The outlier case means that we can not readily discard consideration of *low* belief regions, since it may be attributable to an unfortunate erroneous measurement early-on.

In practical scenarios, we find indoor room scenes to comprise of at least one large open space. In these cases, the enclosed area of the floor-plan greatly exceeds the perimeter of the delineating outline. A classical grid-based localization technique would need to consider every interior cell of the model and perform a large up-front ray-casting operation; thereby working from the *inside-out* Thrun et al. (2005). In contrast, due to the computational load, we opt to instead discretize the perimeter of the floor plan, e.g., walls, and work from the *outside-in*. A reasonable discretization of the perimeter can be significantly smaller than the encompassing area. The discretization can be carried out very quickly, since it only requires traversing a series of line segments. We can construct a lookup table for each discrete point along the perimeter which stores the position of the model centroid relative the point position, $(-x_m^d, -y_m^d)$. We assume the model to be centered at the origin. We also store the outward-facing normal at each discrete point (n_x^d, n_y^d) . This fast lookup table construction process is repeated for $|N_\xi|$ rotated versions of the model, to construct a table $\text{LUT}(d, \xi)$ similar to an R-table in the GHT algorithm.

Given a new observation, we iterate through our table $\text{LUT}(d, \xi)$ for each discrete point and possible rotation. We perform several pre-filtering checks to confirm whether we need to accumulate a vote based on feasibility conditions such as the hypothesized pose being within the model and the incidence angle being feasible. Hence, we avoid unnecessary computation both online as well as via any large up-front pre-computations. We outline the preconditions in Algorithm 1 and our voting scheme in Algorithm 2.

The localization algorithm is a voting-based algorithm; hence, it is able to cope with multi-modal belief spaces. Classical Bayesian approaches to localization (Thrun et al., 2005) can suffer in the pres-

Algorithm Stage	Classical Approach	Our Approach
Ray-Casting Precomputations	$O(E A N_\xi)$	N/A
R-table Construction	N/A	$O(E D N_\xi)$
Preconditions	N/A	$O(D N_\xi)$
Accumulation (LUTs)	$O(A N_\xi)$	$O(D N_\xi)$
Total	$O((E A N_\xi + A N_\xi))$	$O(E D N_\xi + D N_\xi)$

Table 1: Computational comparison between our approach and classical approach to grid-based localization with fixed-grid size. We assume we consider the full belief space at each iteration, since we consider a sparse number of measurements and possible outliers. The computational difference stems from the size of the area of the floor-plan A versus the resolution of the perimeter discretization D . For the majority of floor-plans, a large open area surrounds the visual center of the floor-plan model; hence, a convex approximation of this space can clearly illustrate the computational advantage of our approach for a limited set of measurements. Our computation for each accumulation phase is slightly larger; however, our up-front cost is dramatically less. Especially for cases of dynamic map models, where only a small number of measurements are made with a given map configuration under consideration, our approach can be seen to be more efficient.

ence of outliers, due to the tendency for erroneous likelihoods to *null* the posterior resulting in the permanent loss of information. Most of these methods will attempt to cope with outliers via additive non-informative priors to account for outliers in the measurement likelihood distribution (i.e., an additive small uniform probability), which prevents zeroing of the belief space. Contrarily, a voting-based approach is *non-destructive* and hence can accommodate a high percentage of outliers.

Our algorithm also checks several preconditions prior to accumulating a given vote into the belief space which further helps handle outliers. The preconditions are sanity checks: require that the measurement originate from within the model (i.e., feasible measurement given assumption sensor is within model) and require the incidence angle of the measurement with the model surface is within a certain tolerance of the surface normal (i.e., obtuse incidence angles can be pruned, since they are unlikely to have returned sufficiently strong sensor signal).

We present a side-by-side computational order comparison with classical approaches (Fox et al., 1998) in Table 1.

Algorithm 1: Check Preconditions

Result: Whether to accumulate a vote
Given an input sample measurement;
for $\xi \in N_\xi$ **do**
 if *Scene normal* (n_x^d, n_y^d) *feasible given sample* **then**
 if *Hypothetical agent pose relative scene lies within model* **then**
 Vote for Sample, Algorithm 2
 end
 end
end

Algorithm 2: Accumulate Vote

Result: Whether to accumulate a vote
Given input sample measurement and rotation angle of model;
for *neighbourhood of vote location* **do**
 Compute vote-weight at neighbourhood point, based on measurement model of sensor;
 Compute spatial proximity weight for location;
 Compute rotational proximity weight for location;
 Add combined vote-weight to location;
end

3.3 Sparse registration

Once a coarse registration of the floor-plan model has been made against the current scene, we use a sparse-registration strategy to refine the registration estimate. The sparse-registration performs an iterative process similar to ICP; whereby, we alternate between phases of correspondence-matching and optimization over the pose of the model. Algorithm 3 details our workflow for sparse-registration. As with classical point-set registration techniques, the optimization is prone to converging to local optima or flat regions in the registration error function due to the non-linear correspondence matching. Our sparse registration follows a similar workflow to Arun Srivatsan et al. (2019) by perturbing our solution after every optimization routine. We anneal the perturbations gradually in magnitude as the registration routine approaches an optima.

The inner-optimization routine performs an ICP algorithm, which solves for the registration pose \mathbf{T} of the model given a set of observations $\{\mathbf{o}_i \in O\}_{i=0}^{N_o}$. We perform correspondence-matching by projecting each observation \mathbf{o}_i to the nearest point on the model \mathcal{M} , while satisfying a set of constraints \mathcal{C} . If the

set of feasible points is empty, we relax the constraints and opt for the nearest point, albeit with a lower weight assignment to that correspondence. In practice, observations tend to be less reliable when taken at oblique angles to the walls of a surrounding scene. Hence, we weight each correspondence by the cosine of the incidence angle the ray cast of the observation makes with the surface normal. We also constrain the correspondence-matching to search for nearest matches with a more natural incidence angle before considering the more extreme oblique case.

We follow Rusinkiewicz and Levoy (2001) by performing outlier-rejection on any correspondences in the high percentiles in terms of distance error. The optimization routine minimizing the weighted error between our correspondences has an analytical solution for $\hat{\mathbf{T}} \in \mathcal{SE}(2)$,

$$\begin{aligned} \Gamma &= (\mathbf{M} - \bar{\mathbf{m}})^T \mathbf{W} (\mathbf{O} - \bar{\mathbf{o}}) \\ \vartheta &= \arctan \left(\frac{[\Gamma]_{01} - [\Gamma]_{10}}{\text{tr}(\Gamma)} \right) \\ \mathbf{t} &= \bar{\mathbf{o}} - \mathbf{R}_\vartheta \circ \bar{\mathbf{m}}, \end{aligned} \quad (6)$$

where ϑ is the rotation angle between the current model pose and scene, and $\mathbf{M}, \bar{\mathbf{m}}, \mathbf{O}, \bar{\mathbf{o}}$ are the model correspondents (stacked row-wise), the model centroid, the observation correspondents (stacked row-wise), and the observations' centroid, respectively.

Algorithm 3: Sparse Registration

Result: $\hat{\mathbf{T}} \in \mathcal{SE}(2)$
 Given initial estimate $\mathbf{T}_0, k = 0$;
while !converged **do**
 Generate perturbations of estimate;
 $\mathbf{T}_k^i | \mathbf{T}_k + \boldsymbol{\varepsilon}_T \sim \mathcal{N}(0, \boldsymbol{\sigma}); \forall i \in \mathbb{N}_\nu \cup [0, M]$;
 Select $\hat{j} = \arg \min_j \mathcal{E}(\mathbf{T}_k^j)$;
 Solve $\hat{\mathbf{T}}_{k+1} = \text{SparseICP}(\mathbf{T}_k^{\hat{j}})$;
 if $\mathcal{E}(\hat{\mathbf{T}}_{k+1}) < \mathcal{E}(\mathbf{T}_k^{\hat{j}})$ **then**
 $\mathbf{T}_{k+1} = \hat{\mathbf{T}}_{k+1}$;
 else
 $\mathbf{T}_{k+1} = \mathbf{T}_k^{\hat{j}}$;
 end
 Update perturbation $\boldsymbol{\sigma} \propto \sqrt{\mathcal{E}(\mathbf{T}_{k+1})}$;
end

3.4 Evaluation metrics

Due to partial and complete symmetries in our randomly generated floor-plans, we want to avoid penalizing the system for registering model with an equally valid registration. A prototypical example would be a

Algorithm 4: Sparse ICP

Result: $\hat{\mathbf{T}} \in \mathcal{SE}(2)$
 Given initial estimate $\mathbf{T}_0, k = 0$;
while !converged **do**
 Apply transform to model
 $\mathcal{M}_k = \mathbf{T}_k \circ \mathcal{M}_{k-1}$;
 Find correspondences between model and observations;
 $(\mathbf{m}_i, \mathbf{o}_j) | \mathbf{m}_i \sim \mathbf{o}_j, \mathbf{m}_i \in \mathcal{M}_k, \mathbf{o}_j \in \mathcal{O} \forall i, j \in \mathbb{N}_0$;
 Outlier rejection;
 $(\mathbf{m}_i, \mathbf{o}_j) | \|\mathbf{m}_i - \mathbf{o}_j\| < \varepsilon_{\text{reject}}$;
 Optimize
 $\mathbf{T}_{k+1} = \arg \min_{\mathbf{T}} \sum_{i=0}^{N_k-1} \|\mathbf{T} \circ \mathbf{m}_i - \mathbf{o}_i\|_{\omega_i}^2$;
end

square floor-plan, which has four equally valid registrations, in the absence of any user-annotation indicating a preferred option. If we were to provide four different reward signals based on these four equally valid registrations, we would confound the optimization routine which must now harmonize this one-to-many mapping. In this vein, we use the symmetry-aware pose representation of Brégier et al. (2018) for each floor-plan.

We quantify the pose of a floor-plan by a transformation $\mathbf{T} \in \mathcal{SE}(2)$, which maps the outline comprising the floor plan from a canonical *inertial* frame to an *object* frame (Brégier et al., 2018). Each floor-plan belongs to its own group of proper symmetries \mathcal{G} such that the *pose* of the floor-plan is invariant to any transformation belonging to this group. Our prototypical square floor-plan would be invariant to 90° rotations about the centroid. We adopt the *pose-distance* $d^{\mathcal{P}}(\cdot)$ proposed by Brégier et al. (2018) for transformations in $\mathcal{SE}(2)$,

$$\begin{aligned} d^{\mathcal{P}}(\mathcal{P}_1, \mathcal{P}_2) &= \arg \min_{\mathcal{G}_1, \mathcal{G}_2 \in \mathcal{G}} \hat{d}^{\mathcal{P}}(T_1 \circ \mathcal{G}_1, T_2 \circ \mathcal{G}_2) \\ \hat{d}^{\mathcal{P}}(T_1, T_2) &= \sqrt{\frac{1}{L} \int_S \mu_S \|T_1(s) - T_2(s)\|^2 ds}, \end{aligned} \quad (7)$$

where L is the perimeter length of the floor-plan and S is the perimeter of the floor-plan. We can simplify Equation 7 by assuming the floor-plan is centered about its center of mass. In practice, we will choose a reference frame with its origin at the center of mass of the model floor-plan when evaluating the pose-distance between the scene and the registered model. The simplification is as follows,

Proper Symmetry Class	Proper Symmetry Group	Pose Representative
Circular Symmetry	$SO(\infty)$	$\mathbf{t} \in \mathbb{R}^2$
No Proper Symmetry	$\{\mathbf{I}\}$	$(\Lambda e^{i\theta}, \mathbf{t}^T)^T \in \mathbb{R}^4$
Cyclic Symmetry	$\mathbf{R}^{\frac{2k\pi}{n}} k \in \mathbb{Z} \cup [0, n]$	$\{(\Lambda e^{i(\theta + \frac{2k\pi}{n})}, \mathbf{t}^T)^T \in \mathbb{R}^4 k \in \mathbb{Z} \cup [0, n]\}$

Table 2: Table of Pose Representatives in $\mathcal{SE}(2)$ from Brégier et al. (2018)

$$d^{\mathcal{P}}(\mathcal{P}_1, \mathcal{P}_2) = \|\mathbf{t}_1 - \mathbf{t}_2\|^2 \quad (8)$$

$$+ \min_{\mathcal{G}_1, \mathcal{G}_2 \in \mathcal{G}} \frac{1}{L} \int_S \mu s \|\mathbf{R}_1 \mathbf{G}_1(s) - \mathbf{R}_2 \mathbf{G}_2(s)\|^2 ds \quad (9)$$

where we separate a transformation \mathbf{T}_i into its constituent rotational $\mathbf{R}_i \in SO(2)$ and translational $\mathbf{t}_i \in \mathbb{R}^2$ parts. The group of symmetries can be treated as a group of rotations about the center of mass of the object; hence, a group member $\mathcal{G}_j \in \mathcal{G}$ can be reduced to a rotation $\mathbf{G}_j \in SO(2)$.

From Equation, 9, one can show (Brégier et al., 2018) that the pose distance between two transformations can be reduced to the Euclidean norm between two *pose-representatives*. Table 2 demonstrates the pose-representative of a given floor-plan depending on the symmetry class. Historically, attempts at constructing metrics for comparing poses in $\mathcal{SE}(2)$ or $\mathcal{SE}(3)$ had found it difficult to decide how to weight the rotational and translational error. The pose-representative uses the inertia matrix Λ to weight the rotational error,

$$\Lambda = \int \frac{1}{L} \int_S \mu \|s\|^2 ds. \quad (10)$$

When evaluating the pose error in our final registration, we construct a pose-representative for our model and our estimate. The pose-representative necessitates that we detect symmetries present in the floor-plan. We use the symmetry detection algorithm outlined in Wolter et al. (1985). The wall junctions of the floor-plan can be represented as a collection of points $\mathbf{x}_i \in \mathbb{R}^2$. We use an edge-chain to encode the sequence of points by the interior angle of each consecutive triplet of points, i.e. $\mathbf{x}_{i-1}, \mathbf{x}_i, \mathbf{x}_{i+1}$ and the distance to the next point in the chain, i.e., $\|\mathbf{x}_i - \mathbf{x}_{i+1}\|^2$. The encoded sequence is a vector of tuples, i.e., $[s_0, s_1, \dots, s_N]$, where $s_i = (\phi, \rho) \in [0, 2\pi] \times \mathbf{R}^+$.

By constructing the a $2N - 1$ -length sequence, $[s_1, s_2, \dots, s_N, s_0, \dots, s_N]$, we can perform fast symmetry detection by sub-string matching the new sequence against the original encoded sequence. We assign an equivalence class for edge angles $\hat{\phi} \sim \phi, \forall \{\hat{\phi} | \hat{\phi} + \epsilon_\phi \in \phi + j2\pi, j \in \mathbb{Z}\}$, and the equivalence class for edge distances $\hat{\rho} \sim \rho, \forall \{\hat{\rho} | \|\hat{\rho} - \rho\| < \frac{\epsilon_\rho}{\rho}\}$. The equivalence classes provide a bit of freedom to detect *near* symmetries via the soft tolerances, ϵ_ρ and ϵ_ϕ .

3.5 Inspection tool

We release a full simulation environment with our work, which may benefit further research into learning active sampling strategies. Along with the simulation environment and the previously discussed modules (Section 3.3, 3.2, and 3.1), we also provide an inspection tool for debugging learnt strategies. Behaviour learnt via reinforcement learning can be challenging to debug due to the changing system dynamics and state-dependent nature of the system. Hence, we provide a tool which logs a minimal state-trajectory, i.e., a trajectory comprising of the state at each step along the episode, for offline debugging. Our inspection tool can be run on the state-trajectory to visualize the state-representation at each time-step with easily accessible sliders for navigating to the desired time-step. Since the dimensionality of the belief space of the agent pose will, in general, be greater or equal to 3D, we provide a slider for easily navigating along the different channels of the belief space. The most useful debug feature of the inspection tool is the ability to toggle on and off a guided-backpropagation view of the state-space (Springenberg et al., 2014). The selected action at each time-step is used as the target class for the guided-backpropagation; therefore, we are able to see heat-maps on each state component showing the areas of the state most prominent in eliciting the chosen action.

4 EXPERIMENTS

We evaluate our system in the context of fast and accurate model-based sparse-registration within an indoor scene. We consider the 2D floor-plan scenario, since it allows for more concrete analysis on whether our agent is learning effective sampling strategies.

4.1 Dataset

We generate floor-plans using our simulation environment. We create floor-plans of single rooms based on an underlying non-convex polygonal model. Each floor-plan can be seeded by a random 32bit integer; hence, we generate a training and evaluation set of seed indices. We compute the floor-plans *on-the-fly* during the training process, which facilitates quicker

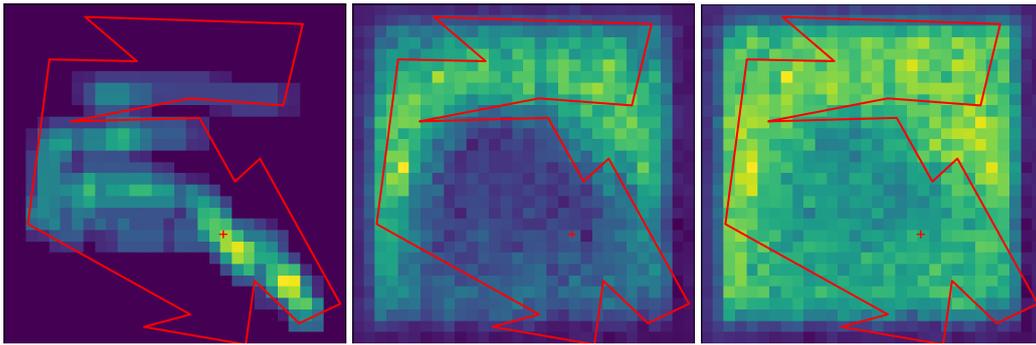


Figure 4: We use our inspection tool to slide through each time-step of a given active sampling episode. The inspector tool uses Guided Back-Propagation Springenberg et al. (2014) to show which areas of the input belief map (left) are active when the agent selects the measurement action (middle), or a rotation action (right). Evidently, the agent has learnt to use the belief map as a form of prior on the agent pose (or coarse registration). We can interpret the activations as the following: If the belief map indicates the agent is likely to be in an unexpected region of the scene, i.e., far from the visual center, it encourages the agent to take more measurements. Similarly, the agent is encouraged to explore (rotate) when the current belief has *unexpected* peaks, but not to the same extent as a measurement action. Noteworthy, we have normalized the activations for visualization purposes.

debugging when making small changes to the algorithm.

In our experiments, we configure our observations of the environment to be topological *scans* of only 20 pixels wide, covering a 45° FOV. The reason for the low dimensional observation is primarily due to its portability to the *real-world*. We commonly refer to porting algorithms trained in simulation to the real-world as *bridging the domain gap*. The domain gap is *widened* when training based on simulated high-dimensional raw pixel representations of the environment. The gap can be *narrowed* when an efficient *meta-representation* of the sensor readings can be reliably generalized to the real-world scenario. The low-dimensional topological scans detect wall intersections which could be readily extracted via *passive* edge-detection techniques, assuming no large floor to ceiling occluders. We have this in common with early-work from Active Localization community, albeit with the motivation that the simulation of indicators based topology are much more easily portable and accessible to the real-world scenario.

4.2 Active-sampling experiments

We train our approach on a larger dataset comprising 20,000 simulated floor-plans. The number of translation is set to 30, and we test two cases for the number of rotation bins - 1 and 10. The maximum allotted time to complete a registration is set to 500 actions.

The heuristic approaches are separated into two categories: *blind* agents and *heuristic* agents. The blind agents perform actions based on a fixed probability mass function; hence they effectively ignore any observations or the current system state. The heuristic agents perform different pragmatic strategies which

are intuitively well-suited for localization, such as performing a sensor measurement intermittently with a constant direction of rotation. The different heuristic approaches are defined in Table 3.

We compare our approach against the previously discussed collection of heuristic and blind alternatives. The various sampling strategies are evaluated on a collection of 1000 different floor-plans from a test set. The agent is instantiated randomly about the visual center of the floor-plan as a sample from a uniform distribution with a radius equal to the nearest distance between visual center and any wall of the floor-plan. The agent’s initial rotation is sampled uniformly from $[0, 2\pi]$.

In the first experiment we use the coarse registration error as a termination condition. Therefore, the agent tries to learn an efficient sampling strategy of the scene in order to quickly reduce the uncertainty based on our grid-based localization. We use penalties for each measurement and rotation action undertaken by the agent, with penalties of 0.05 and 0.005, respectively. Evidently, the measurement cost is an order of magnitude larger to represent the disparity between the time needed for a small pose adjustment versus a high-accuracy measurement sample. We provide a standard +1 reward if the agent is able to find a coarse registration in the allotted time, and -1 if the allotted time is exceeded. We use a clipped quadratic reward for minimizing the final registration error below an acceptable threshold. To ensure the agent sufficiently explores the state-space prior to converging on a *good* strategy, we provide an *exploration bonus*, which we decay as the inverse of the visitation frequency (Audibert et al., 2009). We add the exploration bonus to states based on their *episode length*. In

Heuristic	Description
blind-0	Selects left rotation, and depth measurement 75%, and 25% of the time, respectively.
blind-1	Selects left rotation, and depth measurement 50% of the time.
blind-2	Selects right rotation, left rotation, and depth measurement 33%, 33%, and 34% of the time, respectively
heuristic-0	Alternates between a left rotation and depth measurement
heuristic-1	Rotates in only left direction and samples depth measurement every 6 th action
heuristic-2	Rotates in only left direction and samples depth measurement every 18 th action
heuristic-3	Rotates in only left direction and samples depth measurement every 54 th action

Table 3: Definition of Heuristic Approaches

this way, the bonus acts akin to simulated annealing, in that the agent explores lengthier sequences initially before condensing on shorter sequences as the bonus *cools*.

Table 4 shows the comparison results for our learnt strategy against the heuristic approaches. Due to the small number of measurements required to produce a coarse registration of the scene with a known model, we find heuristic approaches provide a competitive benchmark for evaluation.

5 DISCUSSION

5.1 Understanding strategies

Given our learnt active-sampling strategy, we use the inspection tool to glean insights into the behaviour of our policy. The first insight comes from analyzing successful runs of our system and checking which areas of the belief map are *active*, i.e., grid cells responsible for encouraging the agent to take the action it ultimately chooses.

Figure 4 depicts the outline of a generated floor-plan overlaid on activation *heatmaps* for a measurement (middle) and rotation (right) action. The regions of higher activation are shown in brighter shades of yellow, whereas the darker blue shades indicate low activity. Evidently, the heatmap for the measurement action illustrates a tendency for the agent to encourage measurement actions, when there is substantial belief *probability mass* near the periphery of the floor-plan. A similar pattern emerges with the rotation action, albeit to a lesser extent, in that rotation actions are encouraged when the belief map has mass near the periphery, since the agents are initialized about the visual center of the scene. We can interpret this behaviour as the agent learning a prior over the agent initialization within the floor-plan, and encouraging exploratory, i.e., probing behaviour, when the belief map deviates from this expectation. Another indication that the agent is learning effective behaviour comes from its decision to exclusively choose either left rotations or right rotations, but never both within the same episode. This behaviour is arguably beneficial for our experiments, since alternating rotation directions would be inefficient once a certain direction

has been chosen.

5.2 Future work

We use the success of our coarse registration algorithm (Section 3.2 to determine the ground-truth location (i.e., within coarse bounds) as a termination condition on the action sequence. In practice, the ground-truth pose of the agent within the scene is not known; hence, the termination condition is subject to the user’s discretion based on a feedback visualization of the registration. Naturally, once the automatic procedure finds an approximately correct registration and the user signals completion, the system will then perform a refinement step based on the sample measurements which will exceed the accuracy perceptible by the user. The envisioned user-interface is out-of-scope of the current paper, which concentrates on learning efficient sampling strategies. We see this interaction in an Augmented Reality (AR) setting as promising future work.

We note an improved performance margin of our approach over heuristic benchmarks with an increase in the dimensionality of the pose-space. We expect larger performance gains as the complexity of the task increases, as would be the case in the 3D floor-plan setting. We consider the 3D-setting and an expanded evaluation including a variant of AMCL, applicable to our dual-objectives, as future work.

ACKNOWLEDGEMENTS

This work was enabled by the Competence Center VRVis. VRVis is funded by BMVIT, BMWFW, Styria, SFG and Vienna Business Agency under the scope of COMET - Competence Centers for Excellent Technologies (854174) which is managed by FFG. We acknowledge the support of the Natural Sciences and Engineering Research Council of Canada (NSERC) [516801].

REFERENCES

Arun Srivatsan, R., Zevallos, N., Vagdargi, P., and Choset, H. (2019). Registration with a

Sampling Approach	Recognition Rate	Pose-Error	Average # of Measurements	Average # of Rotations
Our approach	0.997 (0.966)	0.0541 (0.0627)	4.084 (8.524)	9.777 (26.552)
blind-0	0.987 (0.862)	0.0595 (0.1740)	5.354 (13.355)	16.214 (39.891)
blind-1	0.977 (0.794)	0.0706 (0.2549)	11.179 (27.894)	11.146 (27.941)
blind-2	0.698 (0.243)	0.2150 (0.8040)	15.468 (28.837)	30.079 (56.506)
heuristic-0	0.989 (0.891)	0.0651 (0.1525)	9.323 (24.026)	8.544 (23.429)
heuristic-1	0.994 (0.940)	0.0507 (0.0921)	3.199 (7.248)	11.539 (32.390)
heuristic-2	0.951 (0.640)	0.0644 (0.3861)	2.439 (4.577)	25.506 (65.097)
heuristic-3	0.639 (0.115)	0.2117 (0.9036)	1.713 (1.961)	54.447 (93.563)

Table 4: Active sampling strategy versus Heuristic Approaches to sampling the scene. We allot each algorithm 100 actions to find a coarse registration of the scene. The non-trivial rotation case, i.e. 10 rotation bins, is shown in parentheses along side the rotation-free, i.e. 1 rotation bin, case. The heuristic methods present a competitive benchmark in the rotation-free case due to the simplicity. Moreover, it presents a good scenario for eliciting insights on the inner workings of the active-sampling strategy. Our approach can be seen to learn effective strategies relative to the pragmatic heuristic approaches as seen in our high recognition rate and low pose-error, i.e. high registration accuracy.

- small number of sparse measurements. *The International Journal of Robotics Research*, page 0278364919842324.
- Audibert, J.-Y., Munos, R., and Szepesvári, C. (2009). Exploration–exploitation tradeoff using variance estimates in multi-armed bandits. *Theoretical Computer Science*, 410(19):1876–1902.
- Ballard, D. H. (1981). Generalizing the hough transform to detect arbitrary shapes. *Pattern recognition*, 13(2):111–122.
- Brégier, R., Devernay, F., Leyrit, L., and Crowley, J. L. (2018). Defining the pose of any 3d rigid object and an associated distance. *International Journal of Computer Vision*, 126(6):571–596.
- Chaplot, D. S., Parisotto, E., and Salakhutdinov, R. (2018). Active neural localization. *arXiv preprint arXiv:1801.08214*.
- Fox, D., Burgard, W., and Thrun, S. (1998). Active markov localization for mobile robots. *Robotics and Autonomous Systems*, 25(3-4):195–207.
- Gelfand, N., Ikemoto, L., Rusinkiewicz, S., and Levoy, M. (2003). Geometrically stable sampling for the icp algorithm. In *International Conference on 3-D Digital Imaging and Modeling, 2003. 3DIM 2003. Proceedings.*, pages 260–267. IEEE.
- Gottipati, S. K., Seo, K., Bhatt, D., Mai, V., Murthy, K., and Paull, L. (2019). Deep active localization. *IEEE Robotics and Automation Letters*, 4(4):4394–4401.
- Kümmerle, R., Triebel, R., Pfaff, P., and Burgard, W. (2008). Monte carlo localization in outdoor terrains using multilevel surface maps. *Journal of Field Robotics*, 25(6-7):346–359.
- Mnih, V., Badia, A. P., Mirza, M., Graves, A., Lillcrap, T., Harley, T., Silver, D., and Kavukcuoglu, K. (2016). Asynchronous methods for deep reinforcement learning. In *International conference on machine learning*, pages 1928–1937.
- Rusinkiewicz, S. and Levoy, M. (2001). Efficient variants of the icp algorithm. In *International Conference on 3-D Digital Imaging and Modeling, 2001. 3DIM 2001. Proceedings.*, volume 1, pages 145–152.
- Schulman, J., Levine, S., Abbeel, P., Jordan, M., and Moritz, P. (2015). Trust region policy optimization. In *International conference on machine learning*, pages 1889–1897.
- Schulman, J., Wolski, F., Dhariwal, P., Radford, A., and Klimov, O. (2017). Proximal policy optimization algorithms. *arXiv preprint arXiv:1707.06347*.
- Springenberg, J. T., Dosovitskiy, A., Brox, T., and Riedmiller, M. (2014). Striving for simplicity: The all convolutional net. *arXiv preprint arXiv:1412.6806*.
- Sutton, R. S. and Barto, A. G. (2018). *Reinforcement learning: An introduction*. MIT press.
- Thrun, S., Burgard, W., and Fox, D. (2005). *Probabilistic robotics*. MIT press.
- Torsello, A., Rodola, E., and Albarelli, A. (2011). Sampling relevant points for surface registration. In *2011 International Conference on 3D Imaging, Modeling, Processing, Visualization and Transmission*, pages 290–295. IEEE.
- Wolter, J. D., Woo, T. C., and Volz, R. A. (1985). Optimal algorithms for symmetry detection in two and three dimensions. *The Visual Computer*, 1(1):37–48.